Dynamic hybrid model for biopesticides production using *Bacillus thuringiensis* strains

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DCAI 2024 June 26th-28th, 2024

International Conference















Outline

- 1. Biopesticides with Bacillus thuringiensis (Bt)
- 2. Proposed hybrid dynamic model
- 3. Results
- 4. Conclusions and perspectives







Biopesticides with Bt



alternative biopesticides for **SAFe** integrated pest and WAter management around Mediterranean



Goal: Industrial production of biopesticides



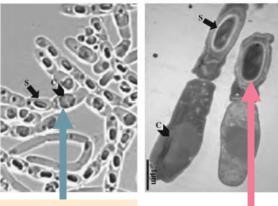








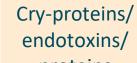
Bacillus thuringiensis (Bt)



proteins

Spores

(Deng et al., 2015)





Modeling approach



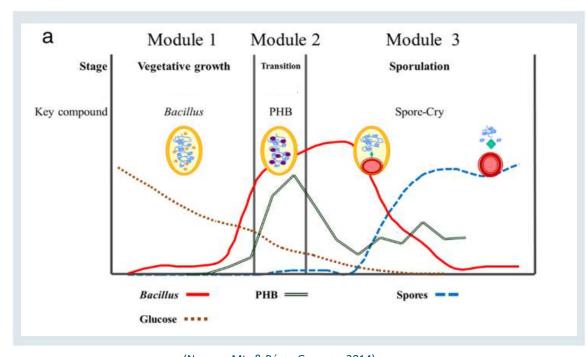




Confidentiel

Modeling of biopesticides by Bt

Bt goes through three main stages in a reactor:



(Navarro-Mtz & Pérez-Guevara, 2014)

There are previous kinetic models

Advantages:

- Presented an accurate description of the biomass production
- Considered oxygen and multiple substrates influence
- Determined that sporulation and protein production are related

Disadvantages:

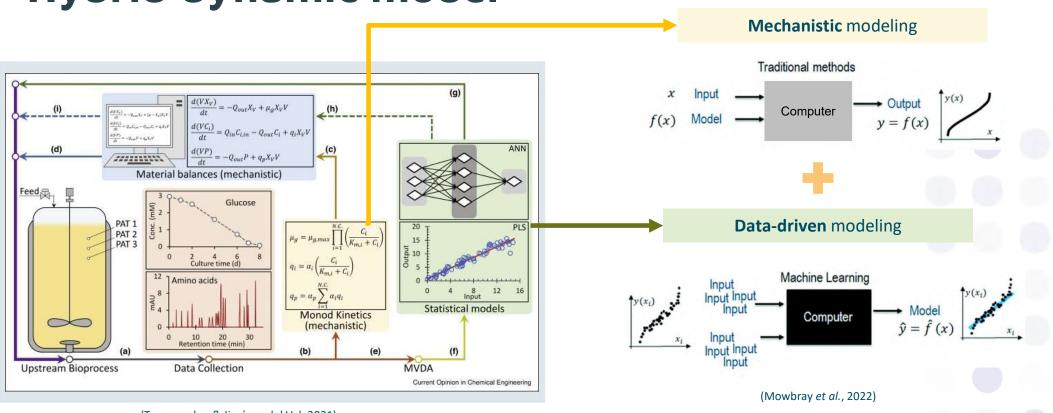
 The protein and spore production has not been properly simulated

We propose a hybrid modeling approach





Hybrid dynamic model



(Tsopanoglou & Jiménez del Val, 2021)

Better for simulating unknown bioprocess mechanisms (e.g. kinetics)

Can consider different operating conditions





Hybrid dynamic model

Mechanistic model



Data driven model

- **Simplified**: few parameters required
- Versatile: small set of data

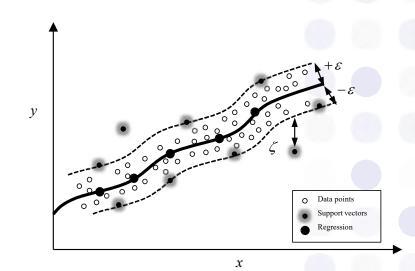
Solves these practical issues:

- Lack of knowledge of biochemical mechanisms
- High costs of frequent sampling and online measurements
- Challenges in pre-determining set-points

Is **limited by** the data quantity and quality

Support Vector Machine (SVM)

$$y = w^T \varphi(x) + b$$







Proposed hybrid dynamic model

Inputs

Mechanistic model

(Monroy et al., 2021)

$$\frac{dX}{dt} = (\mu - k_d) \cdot X$$

$$\frac{dS}{dt} = -\frac{\mu \cdot X}{Y_{XS}} = r_S$$

$$\frac{dPro}{dt} = X \cdot k_{pro} = r_{pro}$$

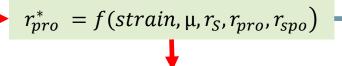
$$\frac{dSpo}{dt} = X \cdot k_{spo} = r_{spo}$$

$$\frac{\mu_{max} \cdot S}{(K_c \cdot X) + S} = \mu$$



Data driven model

SVM regression – Gaussian Kernel



 $r_{spo}^* = f(strain, \mu, r_S, r_{pro}, r_{spo}, r_{pro}^*)$

$$\frac{dSpo}{dt} = r_{spo}^*$$

Recalculation

$$\frac{dP}{d}$$







Data available

Table 1. Inventory of experimental data from lab tests in the project.

Strain 1 (BLB1)		Strain 2 (HD1)		Strain 3 (Lip)	
Batch	Data per variable	Batch	Data per variable	Batch	Data per variable
1	10	4	10	7	26
2	10	5	7	8	8
3	11	6	26	9	10

Training Validation

The validation batches were chosen based on the values of its predictors

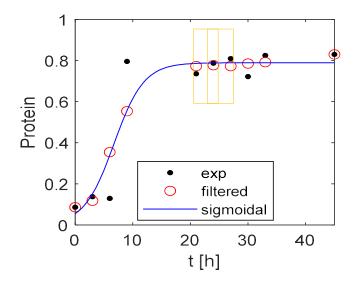




Data filter and sigmoidal function

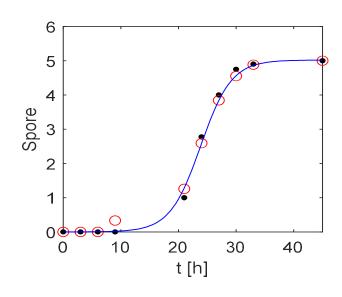
Window median filter

$$y_n = \left(\frac{1}{2 \cdot N + 1}\right) \cdot \sum_{i=n-1}^{n+1} X_i$$



Sigmoidal function

$$f(t) = \frac{1}{a + e^{b + c \cdot t}}$$



100 data points were generated using the sigmoidal function for each training batch



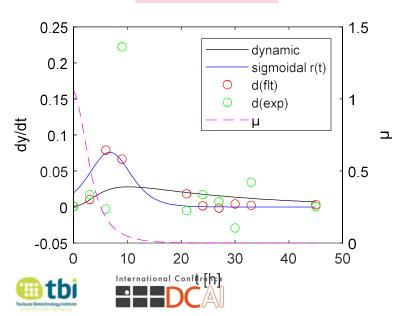


Output and Predictors

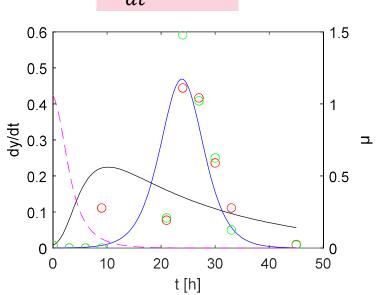
Sigmoidal function derivative

$$\frac{d(f(t))}{dt} = \frac{(-b * e^{b+c \cdot t})}{(a + e^{b+c \cdot t})^2}$$

$$\frac{dPro}{dt} = r_{pro}^*$$



$$\frac{dSpo}{dt} = r_{Spo}^*$$



Inputs (Predictors)

- µ
- rS
- rSpo
- rPro
- strain

SVM

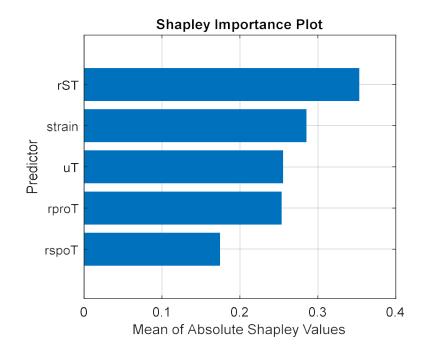
Outputs

- rpro
- rspo

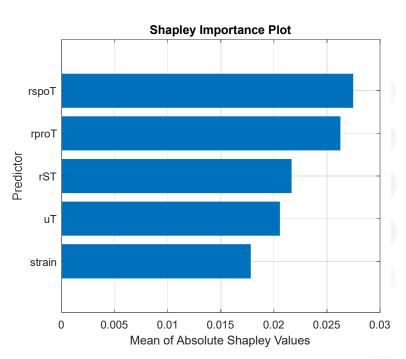
Modeling and optimization of b

Shapley values







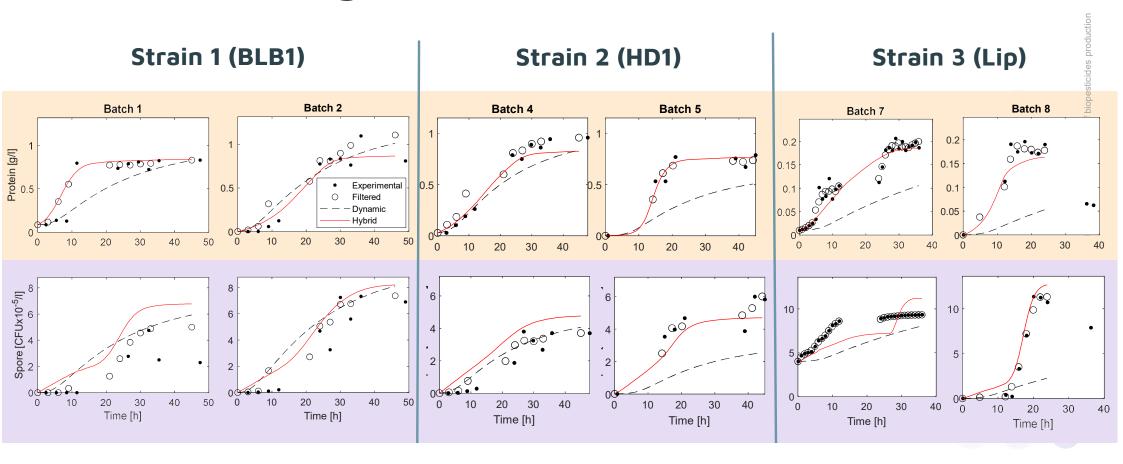


All predictors have significant influence over the model output





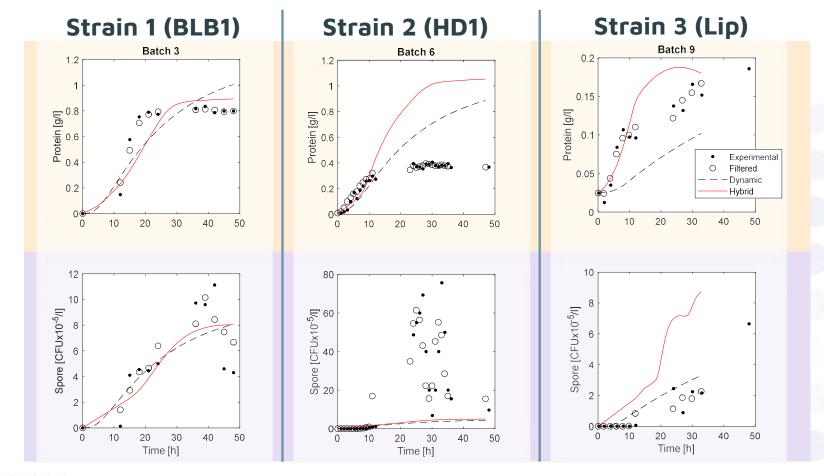
Result training sets







Result validation sets







NRMSE calculation

$$NRMSE = \frac{\sqrt{\frac{1}{n}\sum_{i=1}^{n}(y_i - \hat{y}_i)^2}}{y_{max} - y_{min}}$$

Table 2. NRMSE comparison.

Variable	Data classification	Experimental data	Mechanistic model	Hybrid dynamic model
	Training	Original	0.4231	0.0691
Destais		Filtered	0.4156	0.0540
Protein	Validation	Original	0.4637	0.4049
		Filtered	0.4713	0.4144
	Training	Original	0.4373	0.1143
Sacra		Filtered	0.4340	0.1065
Spore	Validation	Original	0.3067	0.2879
		Filtered	0.3514	0.3262

Improvement

12%

7%





Conclusions



The hybrid dynamic model has improved the prediction of the initial dynamic model

The model requires multiple predictors and they have the same influence

The oxygen influence in the media should be considered in the model

Perspectives

- The model could be enhanced by using more data from other experiments
- The same approach will be consider to simulate **real substrate** conditions
- The **oxygen influence** could be included in the model





Thanks for your attention!

Any questions?

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Acknowledgments. This work was supported by the 'Alternative Biopesticides For Safe Integrated Pest And Water Management Around Mediterranean (SAFWA)' project, which has received funding from the European Union's Horizon 2020 research and innovation program under the grant agreement No2022/Section 2. and the French National Agency for Research Investissements d'Avenir ANR-18-EURE-0021.







Dynamic model for three strains

(Monroy et al., 2021)

$$\frac{dX}{dt} = (\mu - k_d) \cdot X = r_X$$

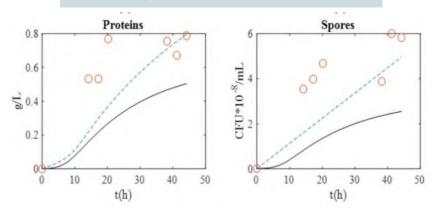
$$\mu = \frac{\mu_{max} \cdot S}{(K_c \cdot X) + S}$$

$$\frac{dS}{dt} = -\frac{\mu \cdot X}{Y_{XS}} = r_S$$

$$\frac{dPro}{dt} = X \cdot k_{pro} = r_{pro}$$

$$\frac{dSpo}{dt} = X \cdot k_{spo} = r_{spo}$$

Training Batch – Strain 02 (HD1)



Validation Batch - Strain 02 (HD1)

